Package 'cobs'

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```
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```

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cobs

COnstrained B-Splines Nonparametric Regression Quantiles

Description

Computes constrained quantile curves using linear or quadratic splines. The median spline $(L_1 \text{ loss})$ is a robust (constrained) smoother.

Usage

Arguments

x vector of covariate; missing values are omitted.

y vector of response variable. It must have the same length as x.

constraint character (string) specifying the kind of constraint; must be one of the values

in the default list above; may be abbreviated. More flexible constraints can be

specified via the pointwise argument (below).

w vector of weights the same length as x (y) assigned to both x and y; default to

all weights being one.

knots vector of locations of the knot mesh; if missing, nknots number of knots will be

created using the specified method and automatic knot selection will be carried out for regression B-spline (lambda=0); if not missing and length(knots)==nknots, the provided knot mesh will be used in the fit and no automatic knot selection will be performed; otherwise, automatic knots selection will be performed on

the provided knots.

nknots maximum number of knots; defaults to 6 for regression B-splines, 20 for smooth-

ing B-splines.

method character string specifying the method for generating nknots number of knots

when knots is not provided; either "quantile" (equally spaced in percentile

levels) or "uniform" (equally spaced knots); defaults to "quantile".

degree degree of the splines; 1 for linear spline (equivalent to L_1 -roughness) and 2 for

quadratic spline (corresponding to L_{∞} roughness); defaults to 2.

tau desired quantile level; defaults to 0.5 (median).

lambda penalty parameter λ

 $\lambda = 0$: no penalty (regression B-spline); $\lambda > 0$: smoothing B-spline with the given λ ;

 $\lambda < 0$: smoothing B-spline with λ chosen by a Schwarz-type information crite-

rion.

ic string indicating the information criterion used in knot deletion and addition for

the regression B-spline method, i.e., when lambda == 0;

"AIC" (Akaike-type, equivalently "aic") or

"SIC" (Schwarz-type, equivalently "BIC", "sic" or "bic"). Defaults to "AIC".

Note that the default was "SIC" up to cobs version 1.1-6 (dec.2008).

knots.add logical indicating if an additional step of stepwise knot addition should be per-

formed for regression B-splines.

repeat.delete.add

logical indicating if an additional step of stepwise knot deletion should be per-

formed for regression B-splines.

pointwise an optional three-column matrix with each row specifies one of the following

constraints:

(1,xi,yi): fitted value at xi will be \geq yi;

(-1,xi,yi): fitted value at xi will be $\leq yi$;

(0,xi,yi): fitted value at xi will be = yi;

(2,xi,yi): derivative of the fitted function at xi will be yi.

keep.data	logical indicating if the x and y input vectors after removing NAs should be kept in the result.
keep.x.ps	logical indicating if the pseudo design matrix \tilde{X} should be returned (as <i>sparse</i> matrix). That is needed for interval prediction, predict.cobs(*, interval=).
print.warn	flag for printing of interactive warning messages; true by default; set to FALSE if performing simulation.
print.mesg	logical flag or integer for printing of intermediate messages; true by default. Probably needs to be set to FALSE in simulations.
trace	integer ≥ 0 indicating how much diagnostics the low-level code in drqssbc2 should print; defaults to print.mesg.
rq.print.warn	flag passed to the fitting function, i.e., either to qbsks2() or directly to drqssbc2().
lambdaSet	numeric vector of lambda values to use for grid search; in that case, defaults to a geometric sequence (a "grid in log scale") from lambda.lo to lambda.hi of length lambda.length.
lambda.lo, lambda.hi	
	lower and upper bound of the grid search for lambda (when lambda < 0). The defaults are meant to keep everything scale-equivariant and are hence using the factor $f = \sigma_x^d$, i.e., f.lambda <- sd(x)^degree. Note however that currently the underlying algorithms in package quantreg are <i>not</i> scale equivariant yet.
lambda.length	number of grid points in the grid search for optimal lambda.
maxiter	upper bound of the number of iterations; defaults to 100.
rq.tol	numeric convergence tolerance for the interior point algorithm called from $rq.fit.sfnc()$ or $rq.fit.sfn()$.
toler.kn	numeric tolerance for shifting the boundary knots outside; defaults to 10^{-6} .
tol.0res	tolerance for testing $ r_i =0$, passed to qbsks2 and drqssbc2.
nk.start	number of starting knots used in automatic knot selection. Defaults to the minimum of 2 knots.

Details

cobs() computes the constraint quantile smoothing B-spline with penalty when lambda is not zero. If lambda < 0, an optimal lambda will be chosen using Schwarz type information criterion.

If lambda > 0, the supplied lambda will be used.

If lambda = 0, cobs computes the constraint quantile regression B-spline with no penalty using the provided knots or those selected by Akaike or Schwarz information criterion.

Value

an object of class cobs, a list with components

call the cobs(..) call used for creation.

tau, degree same as input

constraint as input (but no more abbreviated).

pointwise as input.

coef	B-spline coefficients.	
knots	the final set of knots used in the computation.	
ifl exit code := 1 + ierr and ierr is the error from rq.fit.sfnc (package qua consequently, ifl = 1 means "success"; all other values point to algority problems or failures.		
icyc	length 2: number of cycles taken to achieve convergence for final lambda, and total number of cycles for all lambdas.	
k	the effective dimensionality of the final fit.	
k0 (usually the same)		
x.ps the pseudo design matrix X (as returned by qbsks2).		
resid	vector of residuals from the fit.	
fitted	vector of fitted values from the fit.	
SSy	the sum of squares around centered y (e.g. for computation of \mathbb{R}^2 .)	
lambda the penalty parameter used in the final fit.		
pp.lambda vector of all lambdas used for lambda search when lambda < 0 on input.		
pp.sic	vector of Schwarz information criteria evaluated at pp.lambda; note that it is not quite sure how good these are for determining an optimal lambda.	

References

Ng, P. and Maechler, M. (2007) A Fast and Efficient Implementation of Qualitatively Constrained Quantile Smoothing Splines, *Statistical Modelling* **7(4)**, 315-328.

Koenker, R. and Ng, P. (2005) Inequality Constrained Quantile Regression, *Sankhya, The Indian Journal of Statistics* **67**, 418–440.

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Koenker, R. and Ng, P. (1996) A Remark on Bartels and Conn's Linearly Constrained L1 Algorithm, *ACM Transaction on Mathematical Software* **22**, 493–495.

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics & Data Analysis* **22**, 99–118.

Bartels, R. and Conn A. (1980) Linearly Constrained Discrete L_1 Problems, ACM Transaction on Mathematical Software **6**, 594–608.

A postscript version of the paper that describes the details of COBS can be downloaded from https://www2.nau.edu/PinNg/cobs.html.

See Also

smooth.spline for unconstrained smoothing splines; bs for unconstrained (regression) B-splines.

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Examples

```
x <- seq(-1,3,,150)
y \leftarrow (f.true \leftarrow pnorm(2*x)) + rnorm(150)/10
## specify pointwise constraints (boundary conditions)
con <- rbind(c( 1,min(x),0), # f(min(x)) >= 0
             c(-1, max(x), 1), # f(max(x)) \le 1
             c(0, 0, 0.5))# f(0)
## obtain the median REGRESSION B-spline using automatically selected knots
Rbs <- cobs(x,y, constraint= "increase", pointwise = con)
plot(Rbs, lwd = 2.5)
lines(spline(x, f.true), col = "gray40")
lines(predict(cobs(x,y)), col = "blue")
mtext("cobs(x,y)  # completely unconstrained", 3, col= "blue")
## compute the median SMOOTHING B-spline using automatically chosen lambda
Sbs <- cobs(x,y, constraint="increase", pointwise= con, lambda= -1)
summary(Sbs)
plot(Sbs) ## by default includes SIC ~ lambda
Sb1 <- cobs(x,y, constraint="increase", pointwise= con, lambda= -1,
            degree = 1)
summary(Sb1)
plot(Sb1)
plot(Sb1, which = 2) # only the data + smooth
rug(Sb1$knots, col = 4, lwd = 1.6)# (too many knots)
xx < - seq(min(x) - .2, max(x) + .2, len = 201)
pxx <- predict(Sb1, xx, interval = "both")</pre>
lines(pxx, col = 2)
mtext(" + pointwise and simultaneous 95% - confidence intervals")
matlines(pxx[,1], pxx[,-(1:2)], col= rep(c("green3","blue"), c(2,2)), lty=2)
```

cobs-methods

Methods for COBS Objects

Description

Print, summary and other methods for cobs objects.

Usage

```
## S3 method for class 'cobs'
print(x, digits = getOption("digits"), ...)
## S3 method for class 'cobs'
summary(object, digits = getOption("digits"), ...)
## S3 method for class 'cobs'
```

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```
coef(object, ...)
## S3 method for class 'cobs'
fitted(object, ...)
## S3 method for class 'cobs'
knots(Fn, ...)
## S3 method for class 'cobs'
residuals(object, ...)
```

Arguments

```
x, object, Fn object of class cobs.digits number of digits to use for printing.further arguments passed from and to methods.
```

Details

These are methods for fitted COBS objects, as computed by cobs.

Value

print.cobs() returns its argument invisibly. The coef(), fitted(), knots(), and residuals() methods return a numeric vector.

Author(s)

Martin Maechler

See Also

predict.cobs for the predict method, plot.cobs for the plot method, and cobs for examples.

```
example(cobs)
Sbs # uses print.*
summary(Sbs)
coef(Sbs)
knots(Sbs)
```

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conreg

Convex / Concave Regression

Description

Compute a univariate concave or convex regression, i.e., for given vectors, x, y, w in \mathbb{R}^n , where x has to be strictly sorted $(x_1 < x_2 < \ldots < x_n)$, compute an n-vector m minimizing the weighted sum of squares $\sum_{i=1}^n w_i (y_i - m_i)^2$ under the constraints

$$(m_i - m_{i-1})/(x_i - x_{i-1}) \ge (m_{i+1} - m_i)/(x_{i+1} - x_i),$$

for $1 \le i \le n$ and $m_0 := m_{n+1} := -\infty$, for concavity. For convexity (convex=TRUE), replace \ge by \le and $-\infty$ by $+\infty$.

Usage

```
conreg(x, y = NULL, w = NULL, convex = FALSE,
    method = c("Duembgen06_R", "SR"),
    tol = c(1e-10, 1e-7), maxit = c(500, 20),
    adjTol = TRUE, verbose = FALSE)
```

Arguments

adjTol

verbose

x, y	numeric vectors giving the values of the predictor and response variable. Alternatively a single "plotting" structure (two-column matrix / y-values only / list, etc) can be specified: see xy.coords.
W	for method "Duembgen06_R" only: optional vector of weights of the same length as x ; defaults to all 1.
convex	logical indicating if convex or concave regression is desired.
method	a character string indicating the method used,
	"Duembgen06_R" is an active set method written by Lutz Duembgen (University of Berne, CH) in Matlab in 2006 and translated to R by Martin Maechler.
	"SR" is an R interface to the C code of a Support Reduction algorithm written by Piet Groeneboom (TU Delft, NL) and donated to the cobs package in July 2012.
tol	convergence tolerance(s); do not make this too small!
maxit	maximal number of (outer and inner) iterations of knot selection.

is to be adjusted (increased) in some cases.

tions should be "reported".

(for "Duembgen06_R" only:) logical indicating if the convergence test tolerance

logical or integer indicating if (and how much) knot placement and fitting itera-

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Details

Both algorithms need some numerical tolerances because of rounding errors in computation of finite difference ratios. The active-set "Duembgen06_R" method notably has two different such tolerances which were both $1e-7=10^7$ up to March 2016.

The two default tolerances (and the exact convergence checks) may change in the future, possibly to become more adaptive.

Value

an object of class conreg which is basically a list with components

x sorted (and possibly aggregated) abscissa values x.

y corresponding y values.

w corresponding weights, **only** for "Duembgen06_R".

yf corresponding fitted values.

convex logical indicating if a convex or a concave fit has been computed.

iKnots integer vector giving indices of the *knots*, i.e. locations where the fitted curve has

kinks. Formally, these are exactly those indices where the constraint is fulfilled

strictly, i.e., those i where

$$(m_i - m_{i-1})/(x_i - x_{i-1}) > (m_{i+1} - m_i)/(x_{i+1} - x_i).$$

call the call to conreg() used.

iter integer (vector of length one or two) with the number of iterations used (in the

outer and inner loop for "Duembgen06_R").

Note that there are several methods defined for conreg objects, see predict.conreg or methods(class = "conreg").

Notably print and plot; also predict, residuals, fitted, knots.

Also, interpSplineCon() to construct a more smooth (*cubic*) spline, and isIsplineCon() which checks if the int is strictly concave or convex the same as the conreg() result from which it was constructed.

Author(s)

Lutz Duembgen programmed the original Matlab code in July 2006; Martin Maechler ported it to R, tested, catch infinite loops, added more options, improved tolerance, etc; from April 27, 2007.

See Also

isoreg for isotone (monotone) regression; CRAN packages ftnonpar, cobs, logcondens.

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Examples

```
## Generated data :
N <- 100
f \leftarrow function(X) 4*X*(1 - X)
xx <- seq(0,1, length=501)# for plotting true f()</pre>
set.seed(1)# -> conreg does not give convex cubic
x <- sort(runif(N))</pre>
y <- f(x) + 0.2 * rnorm(N)
plot(x,y, cex = 0.6)
lines(xx, f(xx), col = "blue", lty=2)
rc <- conreg(x,y)</pre>
lines(rc, col = 2, force.iSpl = TRUE)
# 'force.iSpl': force the drawing of the cubic spline through the kinks
title("Concave Regression in R")
y2 <- y
## Trivial cases work too:
(r.1 <- conreg(1,7))
(r.2 <- conreg(1:2,7:6))
(r.3 <- conreg(1:3,c(4:5,1)))
```

conreg-methods

Summary Methods for 'conreg' Objects

Description

Methods for conreg objects

Usage

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```
xlab = "x", ylab = expression(s[c](x)),
sub = "simple concave regression", col.sub = col, ...)
## S3 method for class 'conreg'
predict(object, x, deriv = 0, ...)
## S3 method for class 'conreg'
print(x, digits = max(3, getOption("digits") - 3), ...)
```

Arguments

object, Fn, x an R object of class conreg, i.e., typically the result of conreg(..). For predict(), x is a numeric vector of abscissa values at which to evaluate the concave/convex spline function.

type, col, lwd, xlab, ylab, sub, col.sub

plotting arguments as in plot.default.

show.knots logical indicating the spline knots should be marked additionally.

add.iSpline logical indicating if an *interpolation* spline should be considered for plotting.

This is only used when it is itself concave/convex, unless force.iSpl is TRUE.

force.iSpl logical indicating if an interpolating spline is drawn even when it is not con-

vex/concave.

deriv for predict, integer specifying the derivate to be computed; currently must be

0 or 1.

digits number of significant digits for printing.

... further arguments, potentially passed to methods.

Author(s)

Martin Maechler

See Also

```
conreg, ....
```

```
example(conreg, echo = FALSE)
class(rc) # "conreg"
rc # calls the print method
knots(rc)
plot(rc)
## and now _force_ the not-quite-concave cubic spline :
plot(rc, force.iSpl=TRUE)

xx <- seq(-0.1, 1.1, length=201) # slightly extrapolate
## Get function s(x) and first derivative s'(x) :
yx <- predict(rc, xx)
y1 <- predict(rc, xx, deriv = 1)</pre>
```

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drqssbc2

Regression Quantile Smoothing Spline with Constraints

Description

Estimate the B-spline coefficients for a regression quantile *smoothing* spline with optional constraints, using Ng(1996)'s algorithm.

Usage

Arguments

X	numeric vector, sorted increasingly, the abscissa values	
У	numeric, same length as x, the observations.	
W	numeric vector of weights, same length as x, as in cobs.	
pw	penalty weights vector passed to $11.design2$ or $loo.design2$. FIXME: This is currently unused.	
knots	numeric vector of knots for the splines.	
degree	integer, must be 1 or 2.	
Tlambda	vector of smoothing parameter values λ ; if it is longer than one, an "optimal" value will be selected from these.	
constraint	see cobs (but cannot be abbreviated here).	
ptConstr	list of p oin t wise constraints; notably equal, smaller, greater and gradient are 3-column matrices specifying the respective constraints. May have 0 rows if there are no constraints of the corresponding kind.	
maxiter	maximal number of iterations; defaults to 100.	

drqssbc2

integer or logical indicating the tracing level of the underlying algorithms; not trace much implemented (due to lack of trace in quantreg ...) integer, = n, the number of observations. nrq nl1 integer, number of observations in the 11 norm that correspond to roughness measure (may be zero). integer giving the number of equations. neqc integer giving the number of inequality constraints; of the same length as constraint. niqc integer giving the number of equations and constraints. nvar desired quantile level; defaults to 0.5 (median). tau select.lambda logical indicating if an optimal lambda should be selected from the vector of Tlambda. logical indicating if the pseudo design matrix \tilde{X} should be returned (as *sparse* give.pseudo.x matrix). rq.tol numeric convergence tolerance for the interior point algorithm called from rq.fit.sfnc() or rq.fit.sfn(). Note that (for scale invariance) this has to be in units of y, which the default makes use of. tol.0res tolerance used to check for zero residuals, i.e., $|r_i| < tol * mean(|r_i|)$. logical indicating if warnings should be printed, when the algorithm seems to print.warn have behaved somewhat unexpectedly. logical indicating if warnings should be printed from inside the rq.* function rq.print.warn

Details

This is an auxiliary function for cobs, possibly interesting on its own. Depending on degree, either 11.design2 or loo.design2 are called for construction of the sparse design matrix.

Subsequently, either rq.fit.sfnc or rq.fit.sfn is called as the main "work horse".

This documentation is currently sparse; read the source code!

calls, see below.

Value

a list with components

comp1 Description of 'comp1'
comp2 Description of 'comp2'

Author(s)

Pin Ng; this help page: Martin Maechler.

References

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics & Data Analysis* **22**, 99–118.

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See Also

The main function cobs and its auxiliary qbsks2 which calls drqssbc2() repeatedly.

```
11. design2 and loo. design2; further rq.fit.sfnc and rq.fit.sfn from package quantreg.
```

Examples

```
set.seed(1243)

x <- 1:32

fx <- (x-5)*(x-15)^2*(x-21)

y <- fx + round(rnorm(x,s = 0.25),2)
```

DublinWind

Daily Wind Speeds in Dublin

Description

The DublinWind data frame is basically the time series of daily average wind speeds from 1961 to 1978, measured in Dublin, Ireland. These are 6574 observations (18 full years among which four leap years).

Usage

```
data(DublinWind)
```

Format

This data frame contains the following columns:

speed numeric vector of average daily wind speed in knots

day an integer vector giving the day number of the year, i.e., one of 1:366.

Details

The periodic pattern along the 18 years measured and the autocorrelation are to be taken into account for analysis, see the references. This is Example 3 of the COBS paper.

Source

From shar file available from https://www2.nau.edu/PinNg/cobs.html

Has also been available from Statlib; then, with more variables, e.g., in help(wind, package = "gstat") from CRAN package gstat.

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References

Haslett, J. and Raftery, A. (1989) Space-Time Modelling with Long-Memory Dependence: Assessing Ireland's Wind Power Resource (with Discussion: 22-50). *Applied Statistics* **38**, 1–50. doi:10.2307/2347679

COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Examples

```
data(DublinWind)
str(DublinWind)
plot(speed ~ day, data = DublinWind)# not so nice; want time scale
## transform 'day' to correct "Date" object; and then plot
Dday \leftarrow seq(from = as.Date("1961-01-01"), by = 1,
            length = nrow(DublinWind))
plot(speed ~ Dday, data = DublinWind, type = "1",
     main = paste("DublinWind speed daily data, n=",
                  nrow(DublinWind)))
##--- ~ He & Ng "Example 3" %% much more is in ../tests/wind.R
co.o50 <-
 with(DublinWind, ## use nknots > (default) 6 :
  cobs(day, speed, knots.add = TRUE, constraint= "periodic", nknots = 10,
       tau = .5, method = "uniform"))
summary(co.o50)
lines(Dday, fitted(co.o50), col=2, lwd = 2)
## the periodic "smooth" function - in one period
plot(predict(co.o50), type = "o", cex = 0.2, col=2,
     xlab = "day", ylim = c(0,20)
points(speed ~ day, data = DublinWind, pch = ".")
```

exHe

Small Dataset Example of He

Description

The exHe data frame has 10 rows and 2 columns. It is an example for which smooth.spline cannot be used.

Usage

```
data(exHe)
```

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Format

This data frame contains the following columns:

```
x only values 0, 1, and 2.
```

y 10 randomly generated values

Details

Xuming He wrote about this **JUST FOR FUN:**

I was testing COBS using the following "data". For comparison, I tried smooth.spline in S+. I never got an answer back! No warning messages either. The point is that even the well-tested algorithm like smooth.spline could leave you puzzled.

To tell you the truth, the response values here were generated by white noise. An ideal fitted curve would be a flat line. See for yourself what COBS would do in this case.

Source

Originally found at the bottom of http://ux6.cso.uiuc.edu/~x-he/ftp.html, the web resource directory of Xuming He at the time, say 2006.

See Also

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globtemp

Annual Average Global Surface Temperature

Description

Time Series of length 113 of annual average global surface temperature deviations from 1880 to 1992

Usage

```
data(globtemp)
```

Details

This is Example 1 of the COBS paper, where the hypothesis of a monotonely increasing trend is considered; Koenker and Schorfheide (1994) consider modeling the autocorrelations.

Source

'temp.data' in file 'cobs.shar' available from https://www2.nau.edu/PinNg/cobs.html

References

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

Koenker, R. and Schorfheide F. (1994) Quantile Spline Models for Global Temperature Change; *Climate Change* **28**, 395–404.

```
data(globtemp)
plot(globtemp, main = "Annual Global Temperature Deviations")
str(globtemp)
## forget about time-series, just use numeric vectors:
year <- as.vector(time(globtemp))</pre>
temp <- as.vector(globtemp)</pre>
##---- Code for Figure 1a of He and Ng (1999) ------
a50 <- cobs(year, temp, knots.add = TRUE, degree = 1, constraint = "increase")
summary(a50)
## As suggested in the warning message, we increase the number of knots to 9
a50 <- cobs(year, temp, nknots = 9, knots.add = TRUE, degree = 1,
            constraint = "increase")
summary(a50)
## Here, we use the same knots sequence chosen for the 50th percentile
a10 <- cobs(year, temp, nknots = length(a50$knots), knots = a50$knot,
            degree = 1, tau = 0.1, constraint = "increase")
summary(a10)
```

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interpSplineCon

(Cubic) Interpolation Spline from "conreg"

Description

From a "conreg" object representing a *linear* spline,

interpSplineCon() produces the corresponding (cubic) spline (via package **splines**' interpSpline()) by interpolating at the knots, thus "smoothing the kinks".

isIsplineCon() determines if the spline fulfills the same convexity / concavity constraints as the underlying "conreg" object.

Usage

```
interpSplineCon(object, ...)
isIsplineCon(object, isp, ...)
```

Arguments

```
object an R object as resulting from conreg().
isp optionally, the result of interpSplineCon(object, ...); useful if that is already available in the caller.
... optional further arguments passed to interpSpline().
```

Value

```
interpSplineCon() returns the interpSpline() interpolation spline object.
```

isIsplineCon() is TRUE (or FALSE), indicating if the convexity/concavity constraints are fulfilled (in knot intervals).

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Author(s)

Martin Maechler

See Also

```
conreg, interpSpline.
```

Examples

mk.pt.constr

COBS auxiliary for constructing pointwise constraint specifications

Description

COBS (cobs) auxiliary function for constructing the pointwise constraint specification list from the pointwise 3-column matrix (as used as argument in cobs).

Usage

```
mk.pt.constr(pointwise)
```

Arguments

pointwise numeric 3-column matrix, see pointwise in cobs.

Value

A list with components

```
n.equal number of equality constraintsn.greater number of "greater" constraintsn.smaller number of "smaller" constraintsn.gradient number of gradient constraints
```

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Unless the input pointwise was NULL, the result also has corresponding components:

equal 3-column matrix of equality constraints
greater 3-column matrix of "greater" constraints
smaller 3-column matrix of "smaller" constraints
gradient 3-column matrix of gradient constraints

Author(s)

Martin Maechler

Examples

```
## from ?cobs: x \leftarrow seq(-1,3,,150) con \leftarrow rbind(c(1,min(x),0), # f(min(x)) >= 0 c(-1,max(x),1), # f(max(x)) <= 1 c(0, 0, 0.5))# f(0) = 0.5 r \leftarrow mk.pt.constr(con) str(r)
```

plot.cobs

Plot Method for COBS Objects

Description

The plot method for cobs objects. If there was lambda selection, it provides two plots by default.

Usage

Arguments

object of class cobs.

which integer vector specifying *which* plots should be drawn;

show.k logical indicating if the "effective dimensionality" k should also be shown. Only

applicable when which contains 1.

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```
col, 1.col, k.col

colors for plotting; k.col only applies when show.k is true in the first plot

(which == 1) where 1.col[2] and k.col[2] are only used as well, for denoting

"doubtful" points; col is only used for the 2nd plot (which == 2).

lwd, cex

line width and point size for the 2nd plot (i.e. which == 2).

ylim

y-axis limits, see axis, with a smart default.

xlab, ylab, main

axis annotation; see also axis.

subtit

a vector of length 2, specifying a sub title for each plot (according to which).

further arguments passed and to internal plot methods.
```

Details

plot(.) produces two side-by-side plots in case there was a search for the optimal lambda(which = 1:2), and only the (second) data plus spline curve plot otherwise (which = 2).

Author(s)

Martin Maechler

See Also

There are several other methods for COBS objects, see, e.g. summary.cobs or predict.cobs. cobs for examples.

Examples

```
example(cobs)

plot(Sbs)
plot(fitted(Sbs), resid(Sbs),
    main = "Tukey-Anscombe plot for cobs()",
    sub = deparse(Sbs$call))
```

predict.cobs

Predict method for COBS Fits

Description

Compute predicted values and simultaneous or pointwise confidence bounds for cobs objects.

Usage

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Arguments

object	object of class cobs.
Z	vector of grid points at which the fitted values are evaluated; defaults to an equally spaced grid with nz grid points between minz and maxz. Note that now z may lie outside of the knots interval which was not allowed originally.
deriv	scalar integer specifying (the order of) the derivative that should be computed.
minz	numeric needed if z is not specified; defaults to $\min(x)$ or the first knot if knots are given.
maxz	analogous to minz; defaults to max(x) or the last knot if knots are given.
nz	number of grid points in z if that is not given; defaults to 100.
interval	type of interval calculation, see below
level	confidence level
	further arguments passed to and from methods.

Value

a matrix of predictions and bounds if interval is set (not "none"). The columns are named z, fit, further cb.lo and cb.up for the simultaneous confidence band, and ci.lo and ci.up the pointwise confidence intervals according to specified level.

If z has been specified, it is unchanged in the result.

Author(s)

Martin Maechler, based on He and Ng's code in cobs().

See Also

cobs the model fitting function.

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qbsks2

Quantile B-Spline with Fixed Knots

Description

Compute B-spline coefficients for regression quantile B-spline with stepwise knots selection and quantile B-spline with fixed knots **regression spline**, using Ng (1996)'s algorithm.

Usage

```
qbsks2(x,y,w, pw = 0, knots,nknots, degree,Tlambda, constraint, ptConstr,
    maxiter, trace, nrq, nl1 = 0, neqc, tau, select.lambda,
    ks, do.select,
    knots.add = FALSE, repeat.delete.add = FALSE,
    ic = c("AIC", "BIC", "SIC"),
    give.pseudo.x = TRUE,
    rq.tol = 1e-8, tol.kn = 1e-6, tol.0res = 1e-6,
    print.mesg = TRUE, print.warn = TRUE, rq.print.warn, nk.start)
```

Arguments

Х numeric vector, sorted increasingly, the abscissa values numeric, same length as x, the observations. У numeric vector of weights, same length as x, as in cobs. penalty; typically should be 0 here. рw numeric vector of knots of which nknots will be used. knots nknots number of knots to be used. degree integer specifying polynomial degree; must be 1 or 2. (vector of) smoothing parameter(s) λ , see drqssbc2. Tlambda constraint string (or empty) specifying the global constraints; see cobs. list of pointwise constraints. ptConstr non-negative integer: maximal number of iterations, passed to drqssbc2. maxiter integer or logical indicating the tracing level of the underlying algorithms; not trace implemented (due to lack of trace in quantreg ...) nrq, nl1, neqc integers specifying dimensionalities, directly passed to drqssbc2, see there. desired quantile level (in interval (0, 1)). tau select.lambda passed to drgssbc2, see there. number used as offset in SIC/AIC/BIC. ks do.select logical indicating if knots shall be selected (instead of used as specified). knots.add, repeat.delete.add logicals, see cobs.

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ic information criterion to use, see cobs.

give.pseudo.x logical indicating if the pseudo design matrix \tilde{X} should be returned (as sparse

matrix).

rq. tol numeric convergence tolerance for the interior point algorithm called from rq. fit.sfnc()

or rq.fit.sfn().

tol.kn "tolerance" for shifting the outer knots.

tol.Ores tolerance passed to drqssbc2.

print.mesg an integer indicating how qbsks2() should print message about its current stages.

print.warn flag indicating if and how much warnings and information is to be printed; cur-

rently just passed to drqssbc2.

rq.print.warn flag for **quantreg**'s fitting functions, just passed to drqssbc2. nk.start number of starting knots used in automatic knot selection.

Details

This is an auxiliary function for cobs(*, lambda = 0), possibly interesting on its own. This documentation is currently sparse; read the source code!

Value

a list with components

coef .. fidel ..

k dimensionality of model fit.

if1 integer "flag"; the return code.

icyc integer of length 2, see cobs.

knots the vector of inner knots.

nknots the number of inner knots.

nvar the number of "variables", i.e. unknowns including constraints.

lambda the penalty factor, chosen or given.

pseudo. x the pseudo design matrix X, as returned from drqssbc2.

Author(s)

Pin Ng; this help page: Martin Maechler.

References

Ng, P. (1996) An Algorithm for Quantile Smoothing Splines, *Computational Statistics & Data Analysis* **22**, 99–118.

See also the references in cobs.

See Also

the main function cobs; further drqssbc2 which is called from qbsks2().

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USArmyRoofs

Roof Quality in US Army Bases

Description

The USArmyRoofs data frame has 153 observations of roof sections of US Army bases and 2 columns, age and fci. This is Example 2 of He & Ng (1999).

Usage

```
data(USArmyRoofs)
```

Format

This data frame contains the following columns:

age numeric vector giving the roof's age in years.

fci numeric, giving the FCI, the flash condition index, i.e., the percentage of flashing which is in good condition.

Source

From shar file available from https://www2.nau.edu/PinNg/cobs.html

References

He, X. and Ng, P. (1999) COBS: Qualitatively Constrained Smoothing via Linear Programming; *Computational Statistics* **14**, 315–337.

```
data(USArmyRoofs)
plot(fci ~ age, data = USArmyRoofs, main = "US Army Roofs data")
```

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